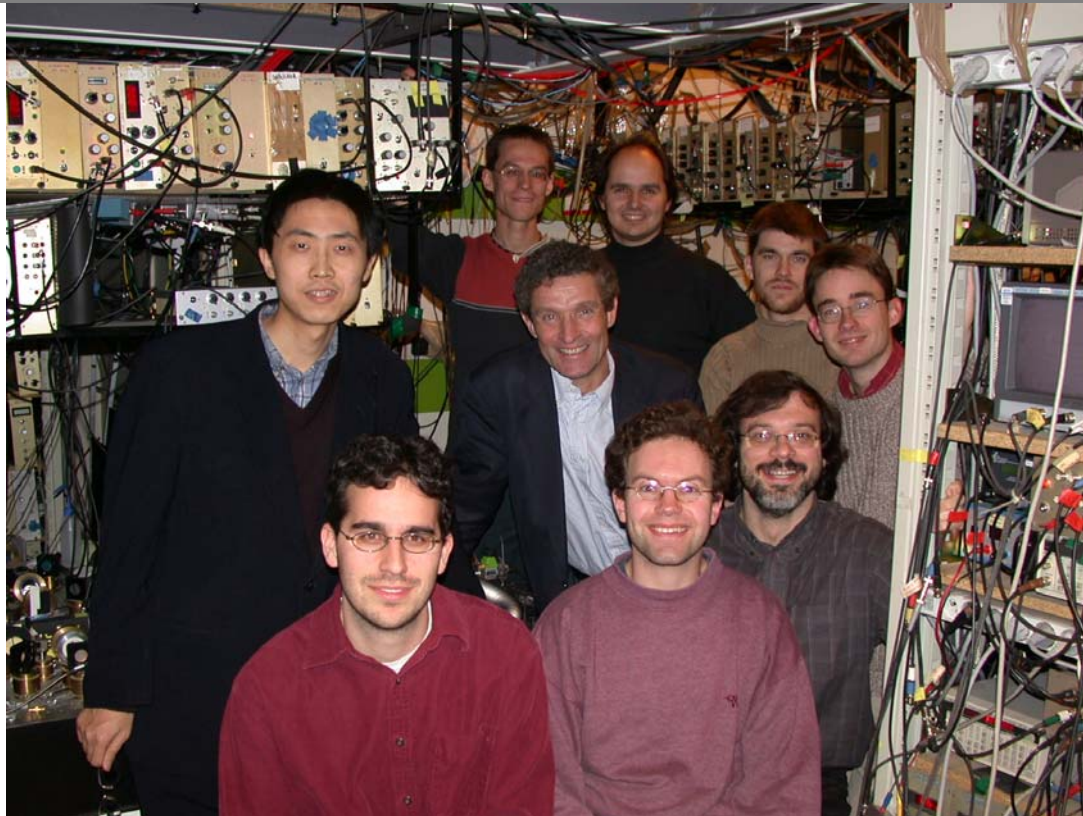


A study of the BEC-BCS crossover region with Lithium 6



1530

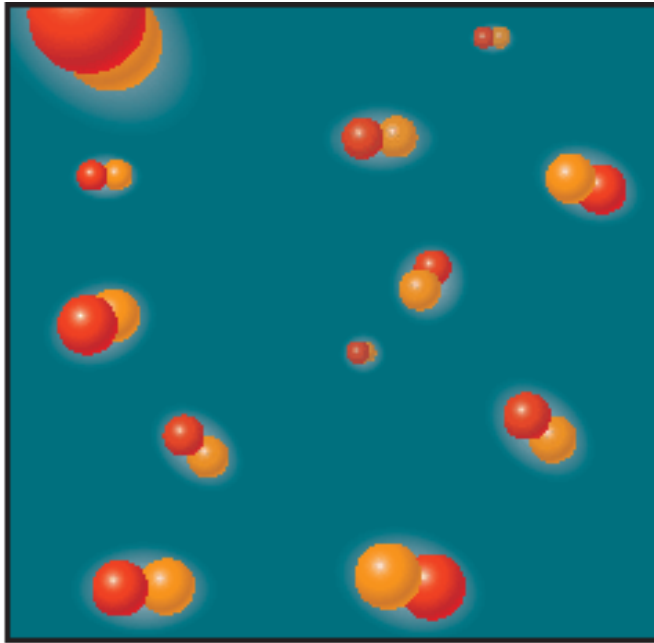
Collège de France

T. Bourdel, L. Khaykovich, J. Cubizolles, J. Zhang, F. Chevy, M. Teichmann, L. Tarruell, S. Kokkelmans, Christophe Salomon
Theory: D. Petrov, G. Shlyapnikov, R. Combescot, Y. Castin
Laboratoire Kastler Brossel, Ecole Normale Supérieure, Paris,
Levico, March 4, 2004

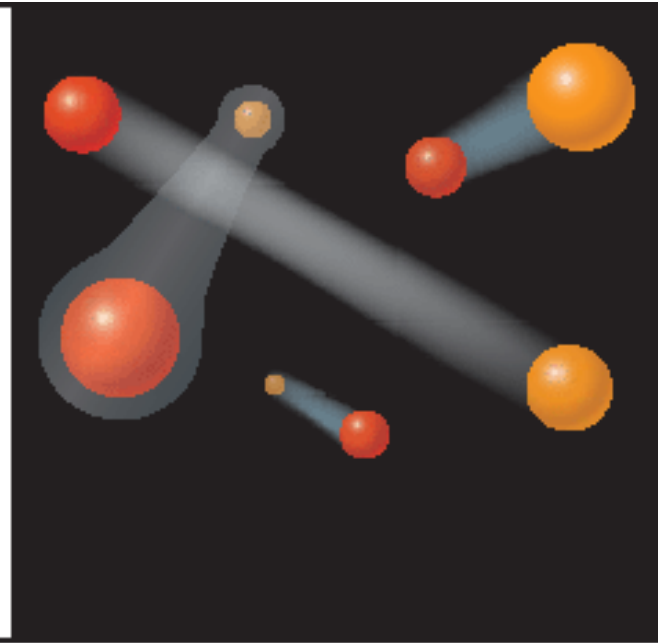
Molecular Bose-Einstein Condensate and Fermi Superfluidity

Two component Fermi gas at very low temperature
s-wave interaction, scattering length a

$a > 0$

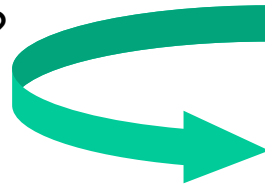


$a < 0$



Molecular BEC ?

Fermi superfluid ?



Feshbach resonance

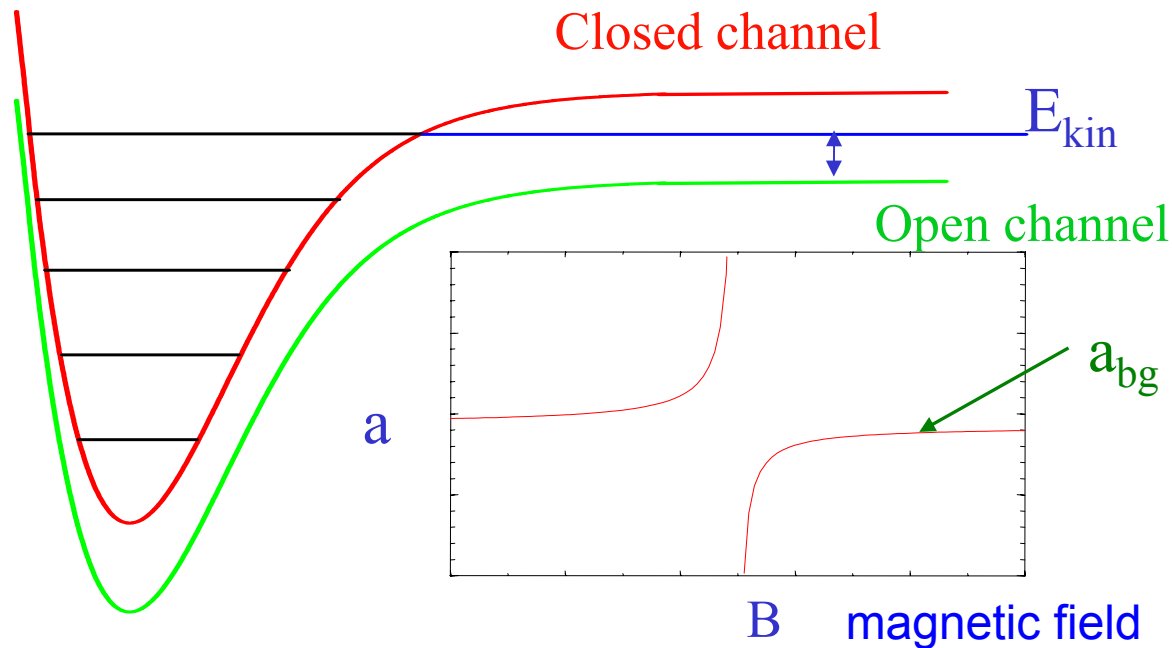
See Science
news focus,
August 8th, 2003

Outline

- Formation and detection of molecules
- Cooling to condensation
- Comparison with other molecular condensates
- Crossover between BEC of molecules and Fermi gas

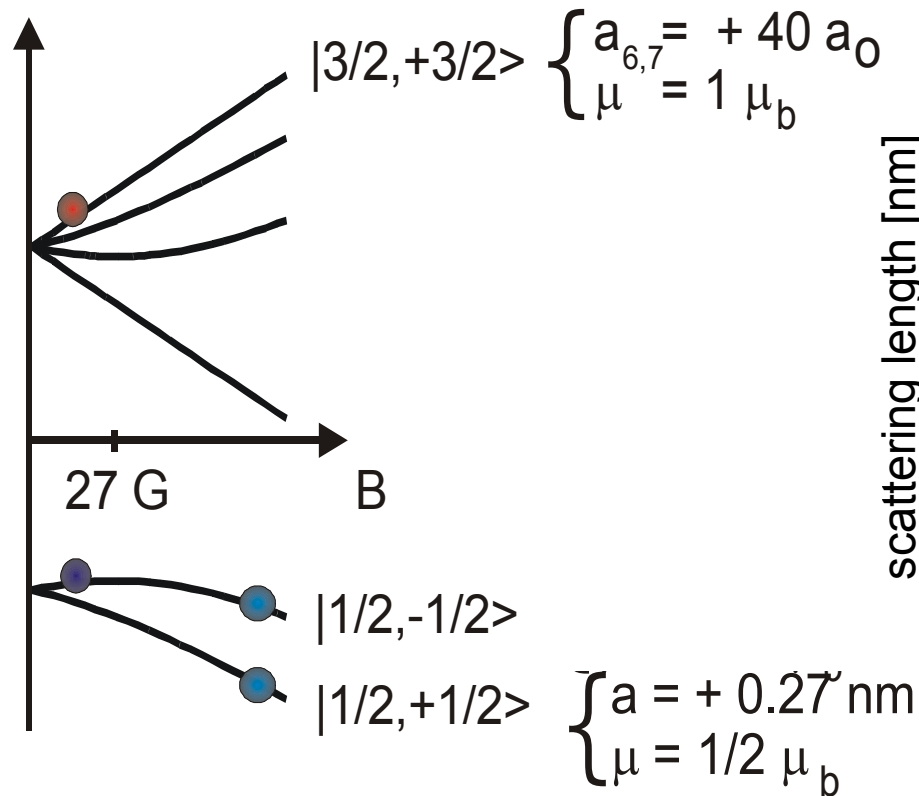
Feshbach Resonance

- Coupling between open channel and closed channel



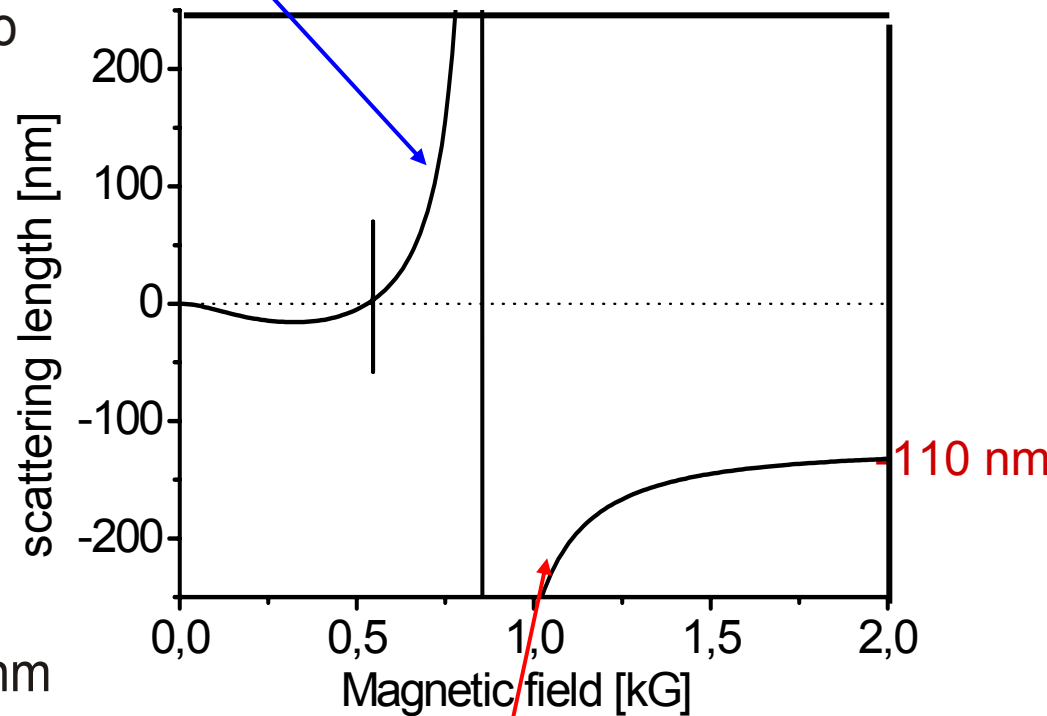
- Resonance: short range molecular state
- What is the lifetime of vibrational levels close to dissociation limit ?
- Scattering is strongly energy dependent

Lithium 6 Feshbach resonance



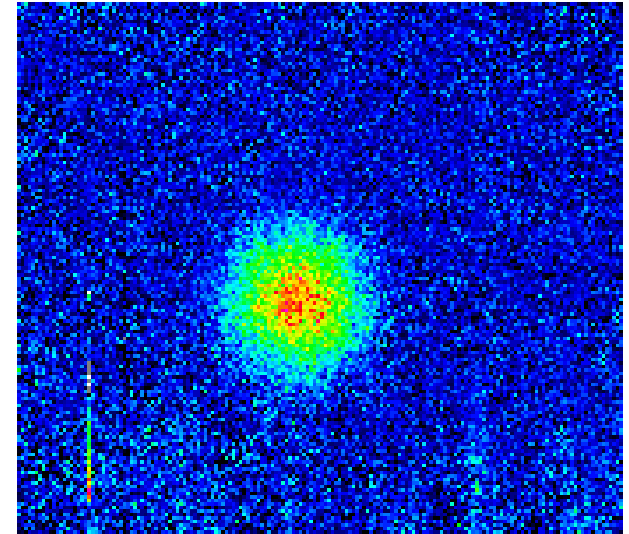
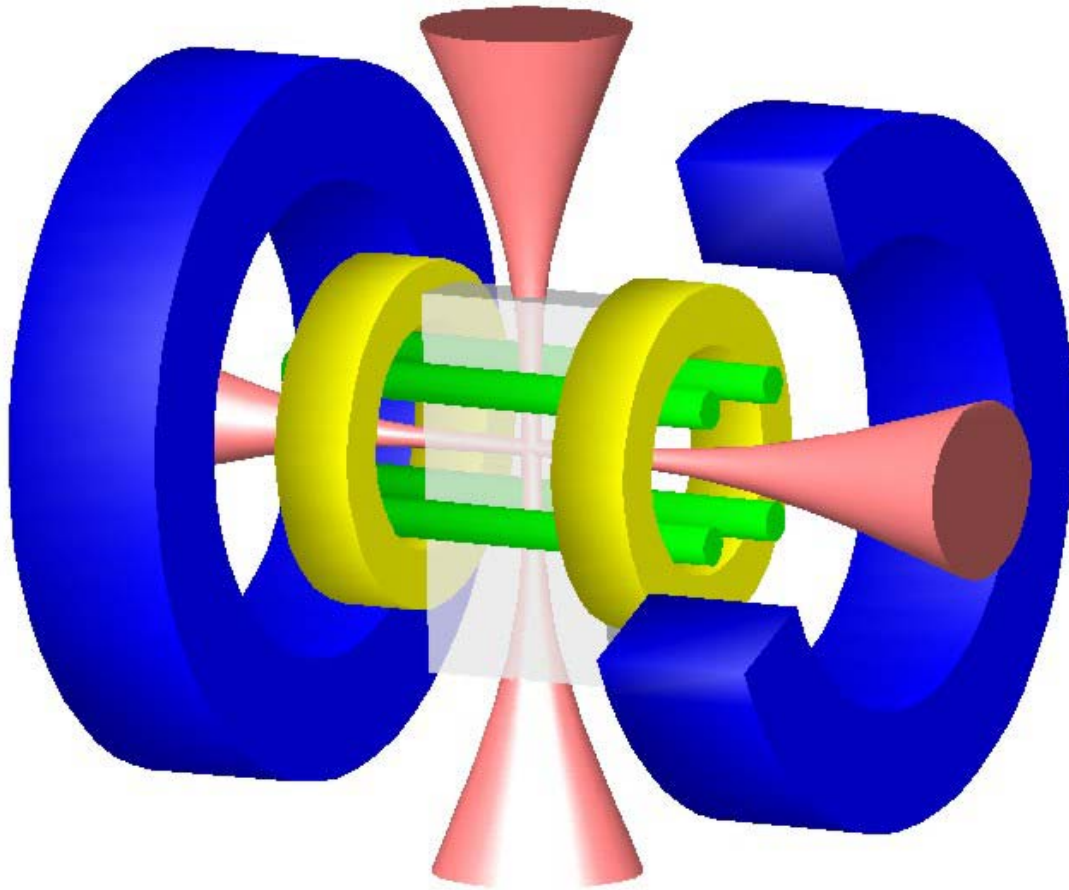
^6Li Lithium

Interesting region
for molecule formation



interesting region for BCS

Strongly interacting ^6Li gas in an optical trap



$$T_F = 2.35 \mu\text{K}$$

$$T/T_F = 0.22$$

$$N_{\text{total}} = 1 \cdot 10^5$$

Two YAG beams
with 2.5 W and waist of $38 \mu\text{m}$

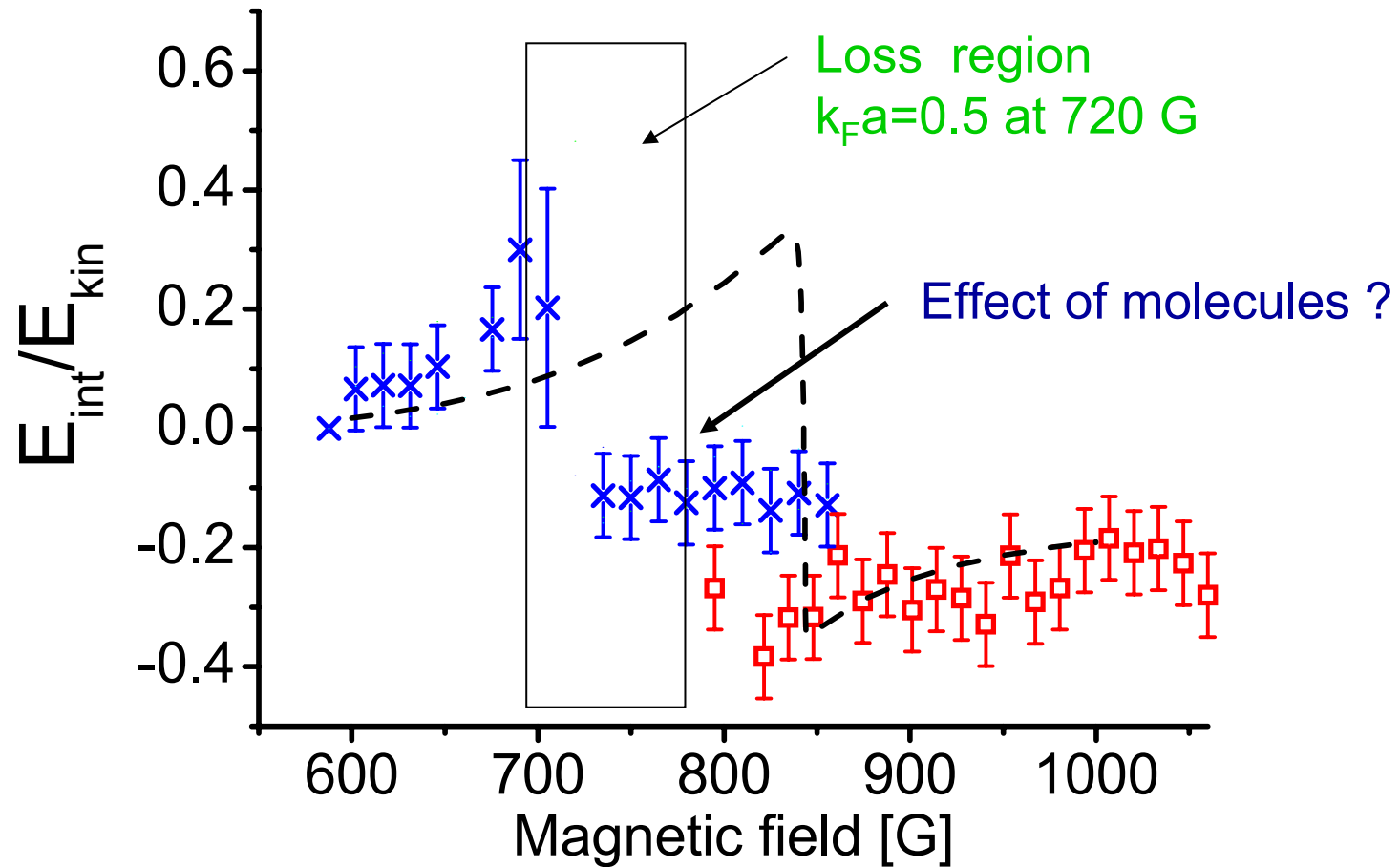
$$E_{\text{interaction}} = -0.35 E_{\text{kin}}$$

$$k_F |a| > 1$$

$$na^3 > 1$$

Bourdel et al., PRL 2003

Interaction energy vs magnetic field: surprises

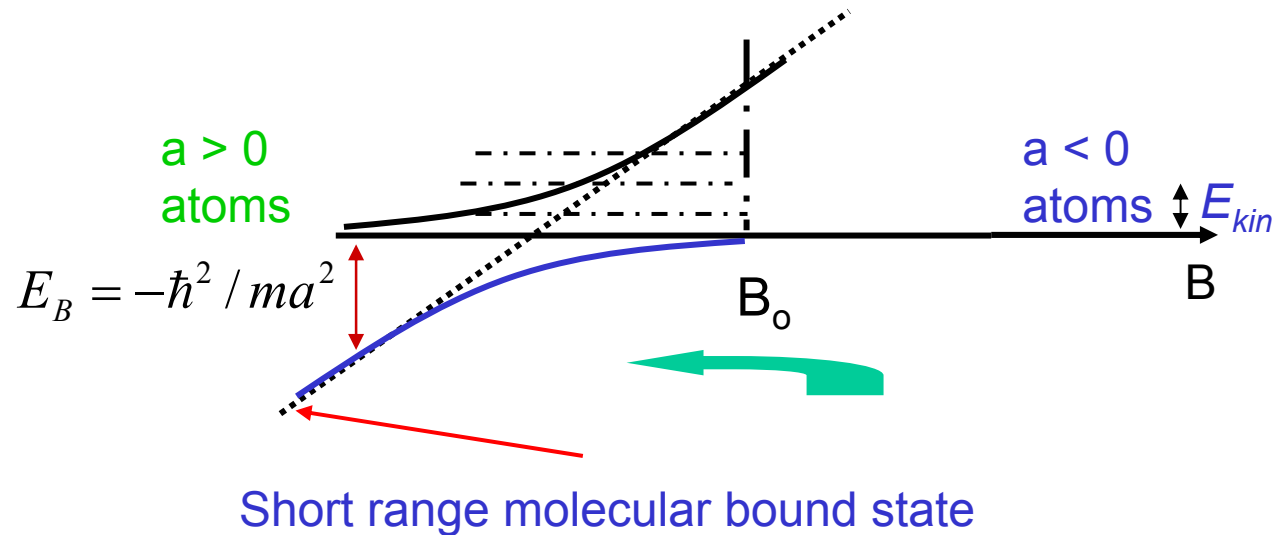


Resonance found at 810(20) Gauss in good agreement with theory
Interaction energy is negative on resonance, as predicted by Heiselberg
Change of sign of E_{int} is shifted from resonance
Strongly interacting Fermi gas: $k_F |a| > 1$

Molecule formation(1): time dependent process

Proposed for bosons in 2000-2001:

Timmermans et al., Verhaar et al., Julienne, Burnett et al.



When crossing the resonance from right to left, it is energetically favorable to form weakly bound molecules with binding energy E_B which remain in the dipole trap

If slow enough, adiabatic and reversible process: entropy is conserved

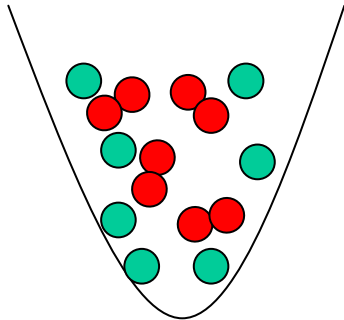
Other method: evaporate fully on the side where a is positive

Molecules formation (2)

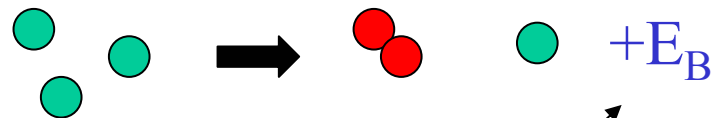
- Three-body recombination [D. Petrov, PRA **67**, 010703 (2003)]
 - Molecules form efficiently in highest weakly bound state

$$\varphi(r) = (r\sqrt{2\pi a})^{-1} \exp(-r/a)$$

Molecules can be trapped!



Binding energy released



$$E_B = \frac{\hbar^2}{ma^2}$$

$$E_B < E_{\text{trap}} \rightarrow$$

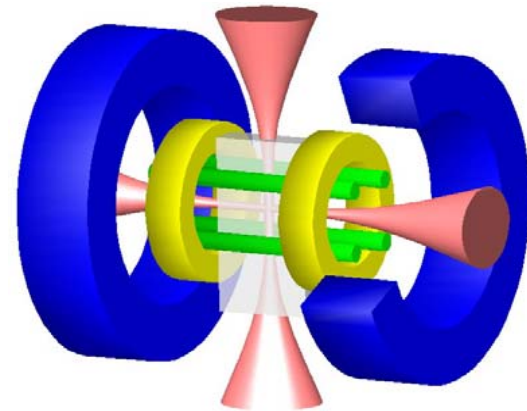
Particles stay in trap with heating

$$E_B > E_{\text{trap}} \rightarrow$$

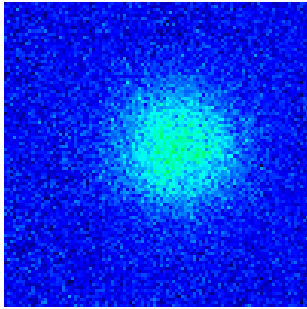
Trap loss

Experimental method for BEC of Li_2 dimers

- Sympathetic cooling of 6Li by 7Li
In magnetic trap until no 7Li left: $10\text{ }\mu\text{K}$
- Transfer into the optical trap
- Transfer from $3/2, 3/2$ to $1/2, 1/2$ by RF adiabatic passage
- Increase the magnetic field to 1060 Gauss ($a < 0$)
- Prepare 50% mixture: $|1/2, 1/2\rangle, |1/2, -1/2\rangle$,
by Zeeman Transfer
- Evaporation of fermions by lowering the trap intensity (factor 10)
- Slow crossing of the Feshbach resonance towards $a = +170\text{ nm}$
in 200 ms . Atoms progressively disappear.
- Further evaporation : pure BEC
- Detection



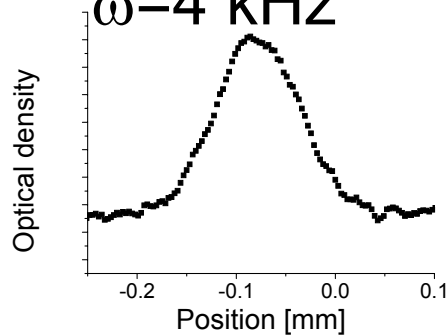
Fermion evaporation



TOF=0.35ms

$N=10^5$

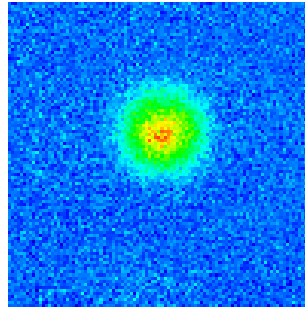
$\omega=4$ kHz



$T=10.5 \mu\text{K}$

$T_F = 12 \mu\text{K}$

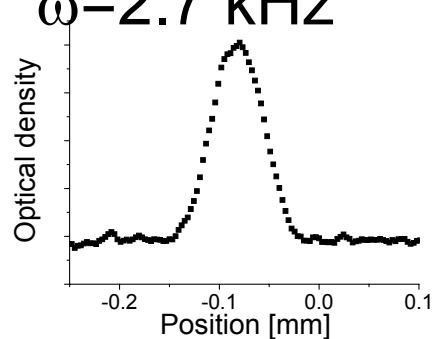
$T/T_F = 0.87$



TOF=0.35 ms

$N=7 \cdot 10^4$

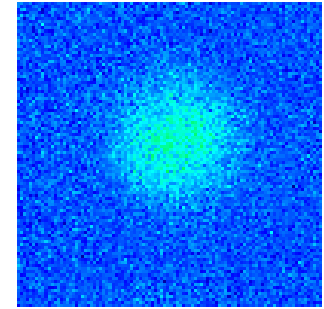
$\omega=2.7$ kHz



$T=3.1 \mu\text{K}$

$T_F = 5.7 \mu\text{K}$

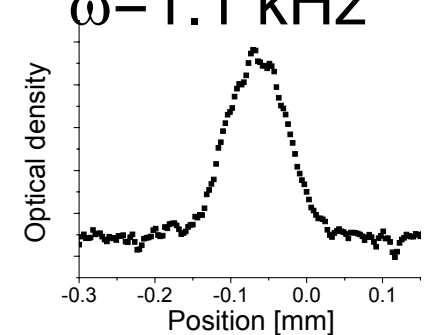
$T/T_F = 0.54$



TOF=1 ms

$N=5 \cdot 10^4$

$\omega=1.1$ kHz



$T < 0.5 \mu\text{K}$

$T_F = 2.5 \mu\text{K}$

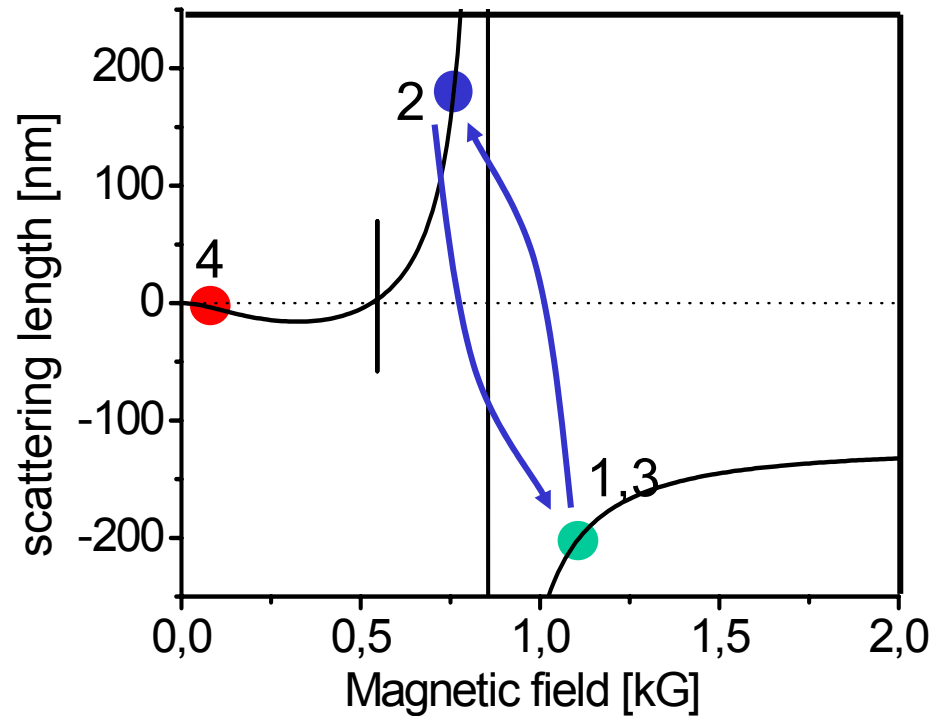
$T/T_F < 0.2$

How to detect molecules ?

For the **probe** laser to be on **resonance**, the magnetic field needs to be **turned off**. **Dimers** follow the B field sweep and are not detected.

Double ramp method :

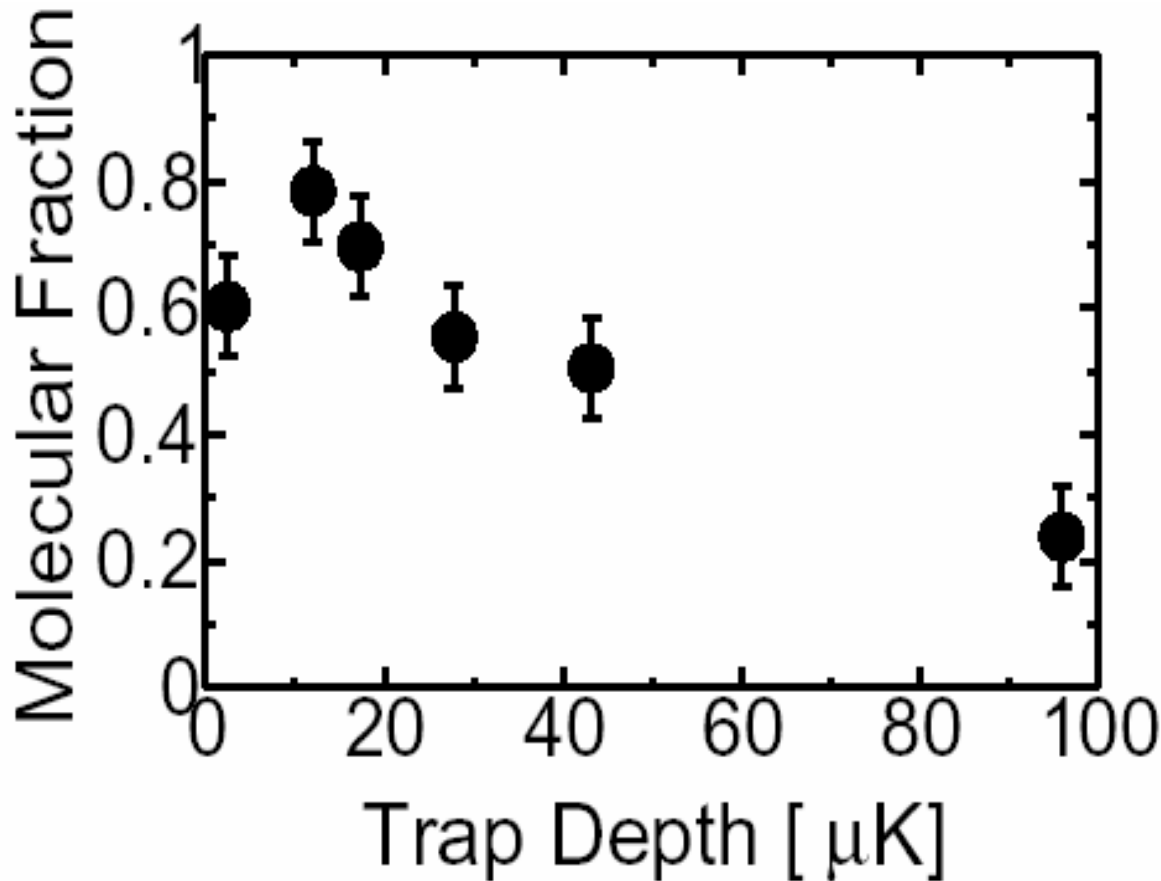
$$2N_{mol} = N_3 - N_2$$



Importance of the ramp speed

Adiabaticity:
$$\frac{1}{E_B} \frac{dE_B}{dt} \ll \frac{E_B}{\hbar}$$

Efficiency of molecule formation influence of trap depth



Most efficient when:
 T/T_F is small and
 T/E_B is small.
The colder the better !

At $B = 689 \text{ G}$

$a = 78 \text{ nm}$

$E_B = 12 \mu\text{K}$

$T_F = 5 \mu\text{K}$

$T = 6.7 \mu\text{K}$

$n_{0m} \sim 4 \cdot 10^{13} \text{ molec/cm}^3$

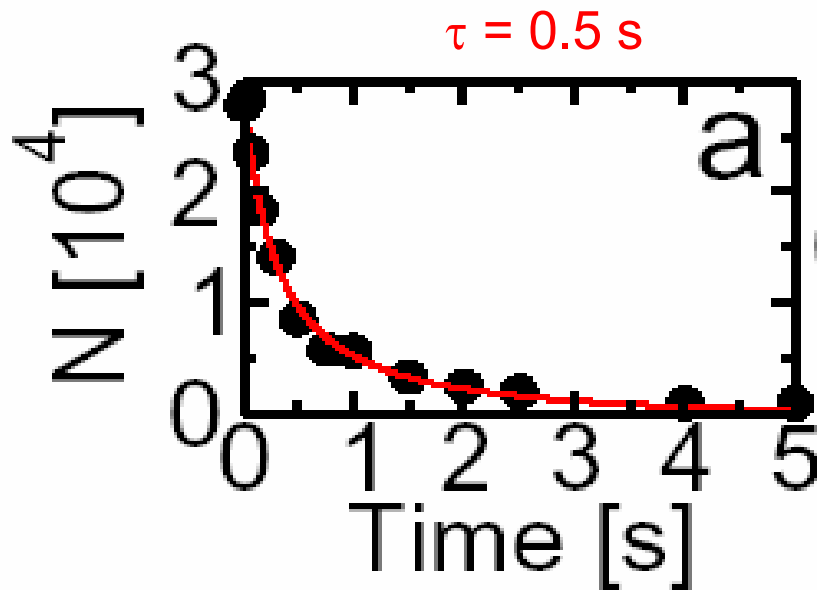
At peak : $3 \cdot 10^4$ cold bosonic molecules

Critical temperature for molecules: $T_C = 3.5 \mu\text{K}$

Factor 2 to gain for BEC of molecules

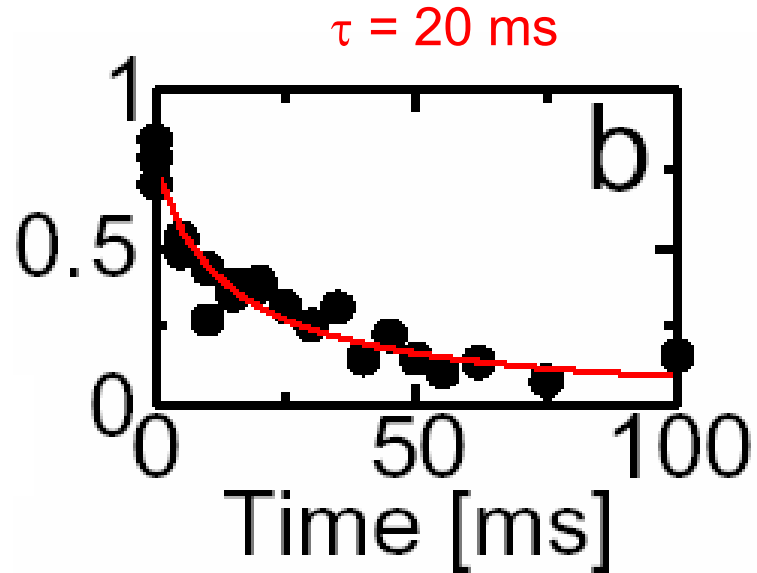
Cubizolles et al.,
PRL, 91, 2003

A good surprise: dimers of
fermions live very long
Strong dependence upon a



$a = 78 \text{ nm}$

Two-body Loss Rate: $\beta \sim 2.4 \cdot 10^{-13} \text{ cm}^3/\text{s}$



$a = 35 \text{ nm}$

The larger is a , the longer the lifetime

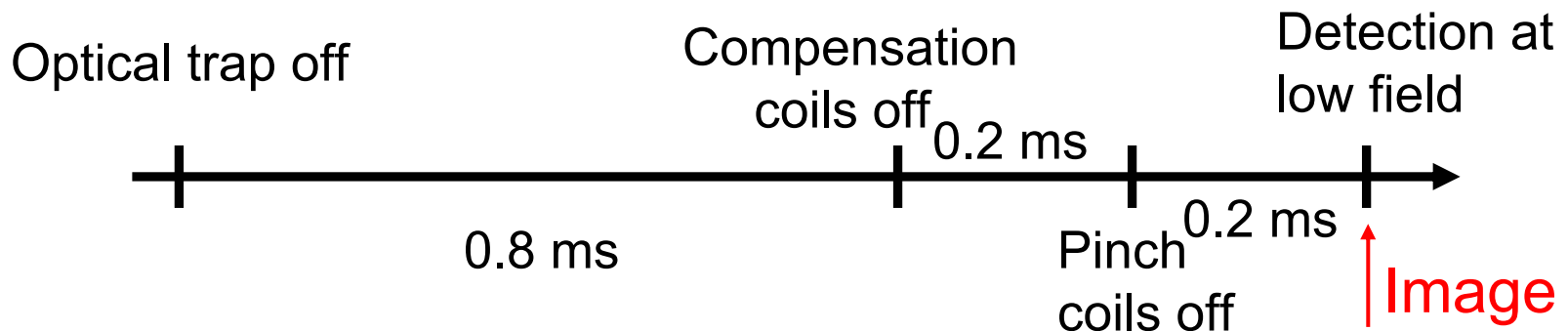
Role of Fermi statistics

$G \sim 1/a^s$ with $s = 2.55$ for dimer-dimer collisions
3.33 for dimer-atom coll.

(D. Petrov, C.S., G. Shlyapnikov)

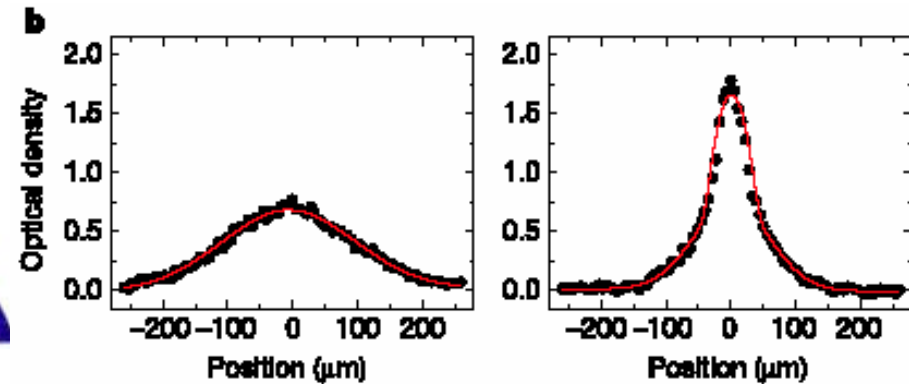
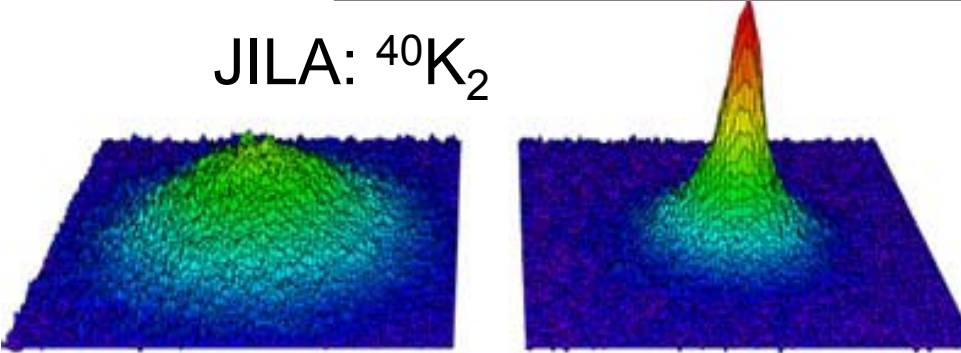
velocity distribution of molecules

- **Low binding energy:** possibility to break the molecules with a fast magnetic field sweep
- If molecule is broken: some extra energy is released
- **High field imaging of molecules and atoms (Innsbruck)**
- **RF dissociation of molecules during TOF (JILA)**
- **Time of flight of molecules (MIT,ENS)**
- Switch off trap and keep B field: molecules expand. Then increase B to break molecules at the last moment. Finally switch to B=0 fast ($20\text{ }\mu\text{s}$)

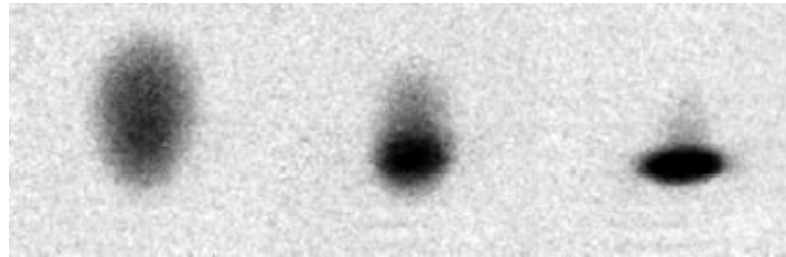


Condensates of molecules

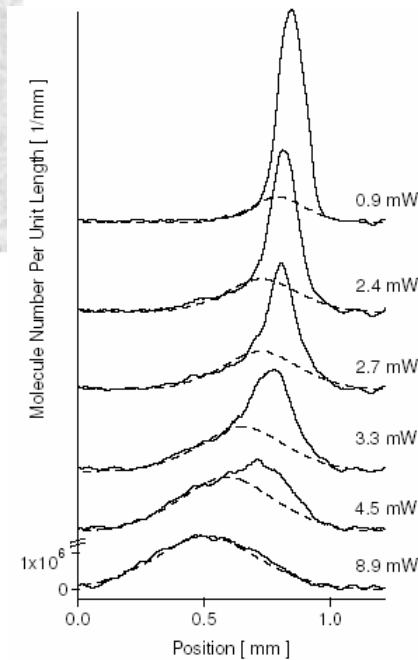
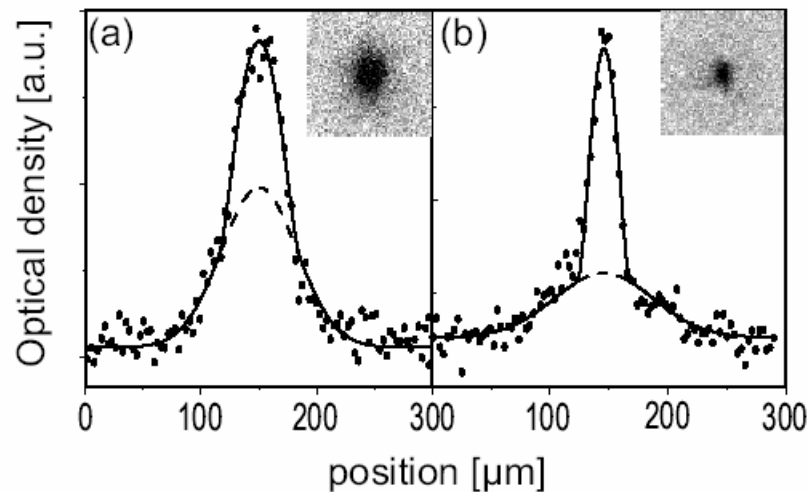
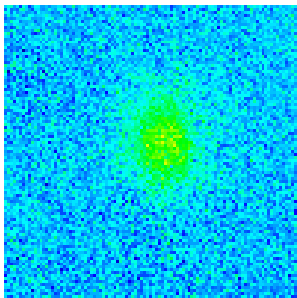
JILA: $^{40}\text{K}_2$



$^6\text{Li}_2$: Innsbruck,
MIT

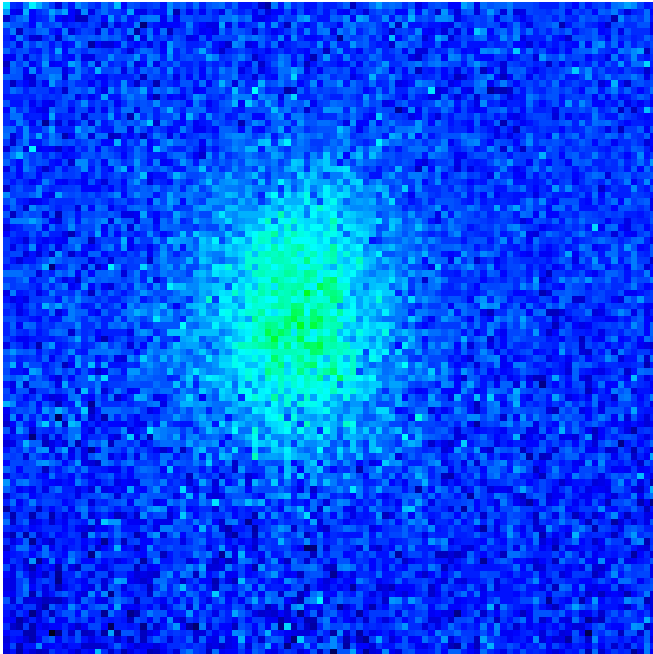


ENS

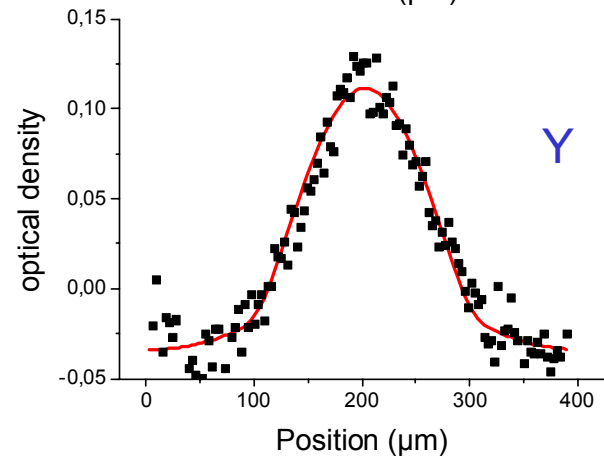
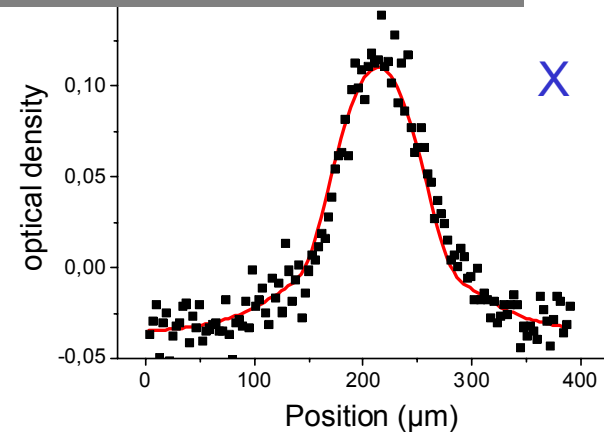


MIT

Bose-Einstein condensation of $^6\text{Li}_2$ molecules



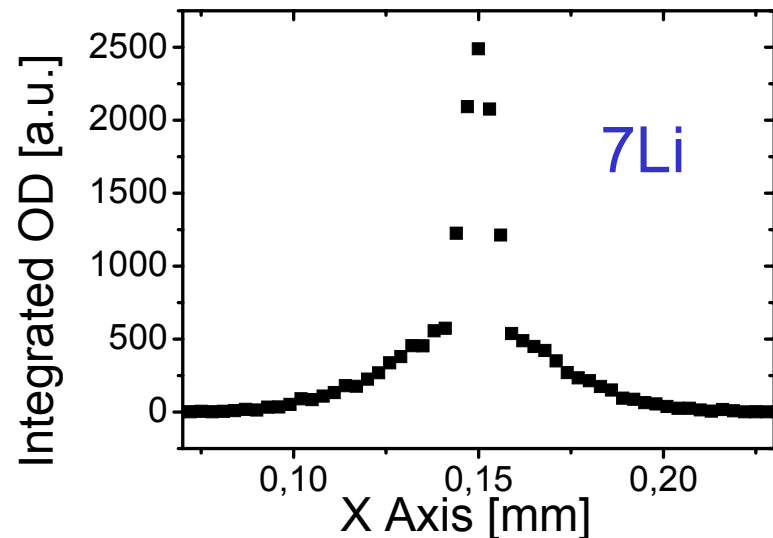
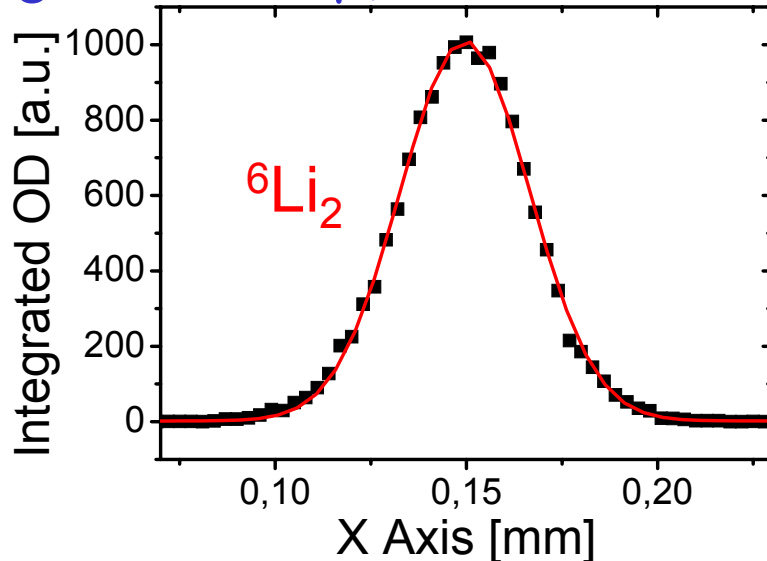
$$\left\{ \begin{array}{l} N = 7.3 \times 10^4 \\ \omega_x = 2\pi \times 1.4 \text{ kHz} \\ \omega_y = 2\pi \times 3.5 \text{ kHz} \\ \omega_z = 2\pi \times 3.8 \text{ kHz} \\ \text{condensed fraction : 33\%} \end{array} \right.$$



Thermal pedestal is visible
 $T_c \sim 1.7 \text{ } \mu\text{K}$ for $1.5 \cdot 10^4$ mol.

Release energy fits

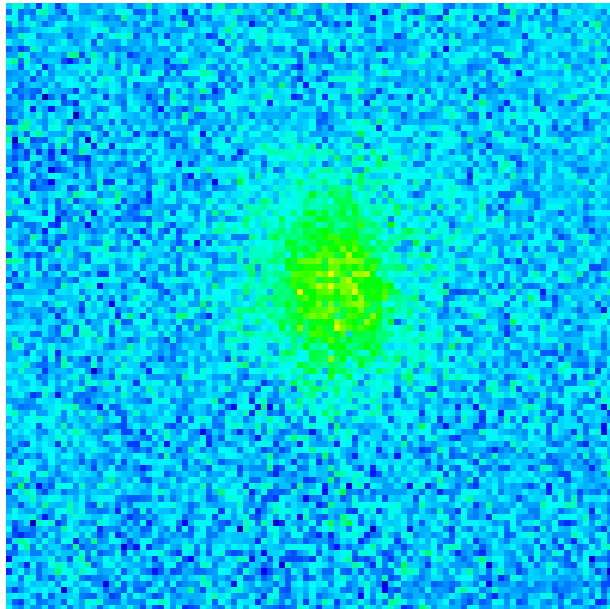
- Model assumption: mean field of the BEC creates an additional potential for the thermal cloud
- Bose distribution of thermal cloud in a new potential is calculated
- Experimental release energy and atom number give T and μ , hence condensed fraction



- $T = 1.1 \mu\text{K} = 0.8 T_c$

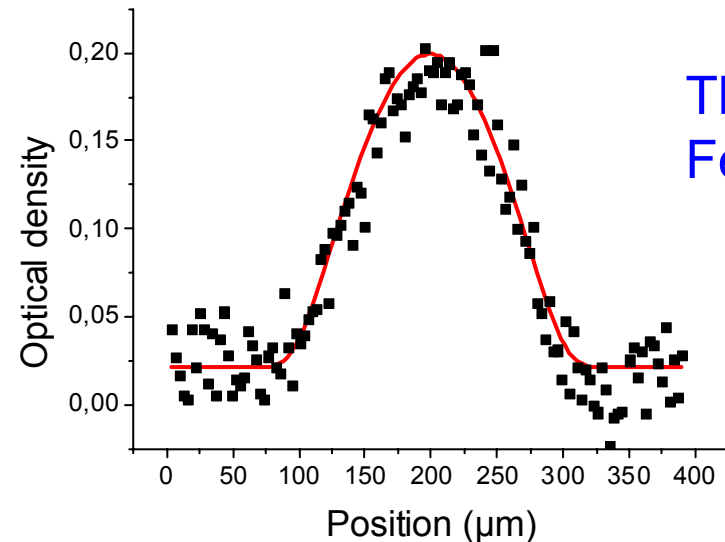
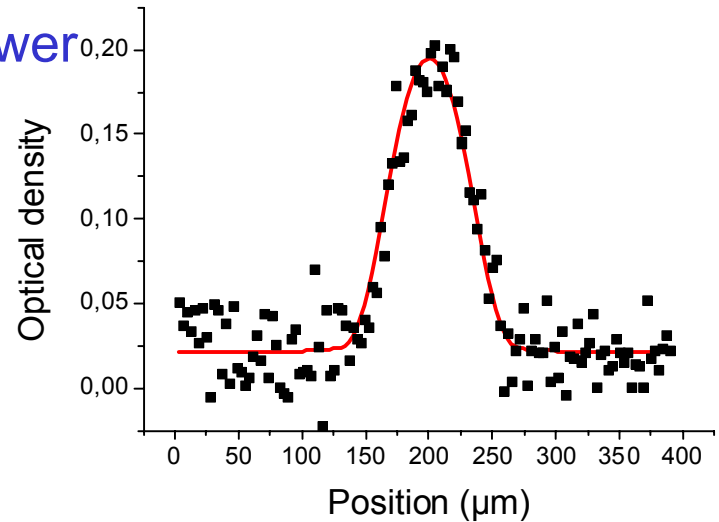
Pure molecular BEC: measurement of a_m

Recompress horizontal beam to full power
 Nearly pure condensate
 No detectable thermal fraction



$$T \leq 0.9 \mu K = T_c^0 / 3$$

$$\begin{cases} N = 3.9 \times 10^4 \\ \omega_x = 2\pi \times 490 \text{ Hz} \\ \omega_y = \omega_z = 2\pi \times 5 \text{ kHz} \end{cases}$$



Thomas
Fermi fit

From expansion

At 770 G $a_{mm} = 170_{-60}^{+100} \text{ nm}$

Strongly interacting condensate

Pure condensate parameters for 770 G, $a_{\text{mm}} = +170$ nm

Theory: $a_{\text{m}} = 0.6a = 0.6 \cdot 306 = 183$ nm D. Petrov, G. Shlyap., C.S.

$2 \cdot 10^4$ molecules in a trap with

Peak density $6 \cdot 10^{13}$ mol/cm³ for $\omega_{\text{bar}} = 2.2$ kHz

$$n_{\text{m}} a_{\text{mm}}^3 = 0.3$$

$$\mu/k_{\text{B}} = 0.8 \text{ } \mu\text{K} = T_{\text{c}}/3$$

Shift of T_{c} by interactions should be easy to study !

Condensate lifetime:

0.3 second at 715 G, $a_{\text{m}} = 66$ nm

3 seconds at 770 G, $a_{\text{m}} = 170$ nm

30 seconds at 1060 G, $a = -167$ nm

Rate constant: $G \sim a^{-1.9 \pm 0.8}$ Theory $G \sim a^{-2.55}$

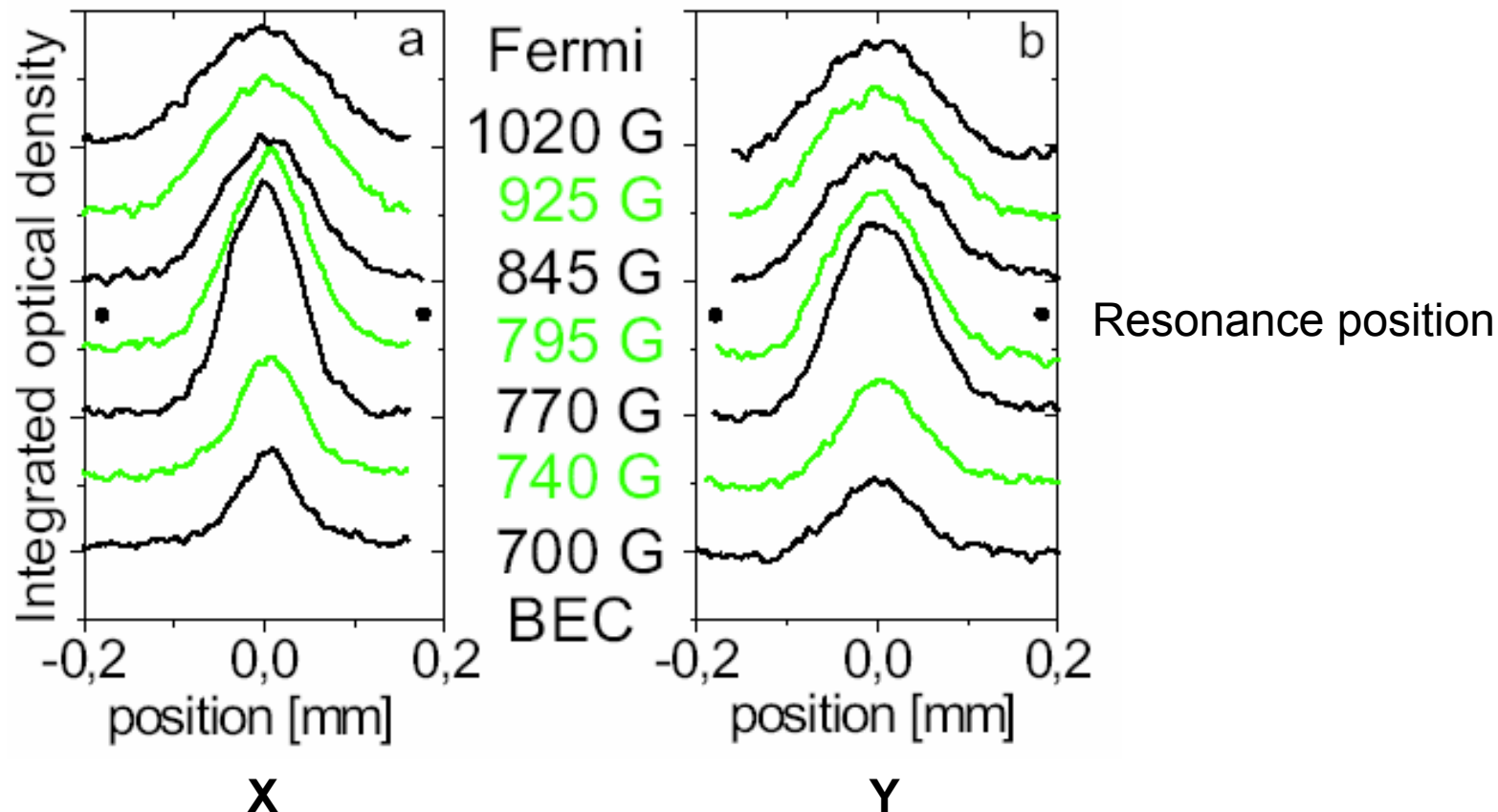
An ideal playground for studying beyond mean field effects

Study of the BEC – BCS crossover region

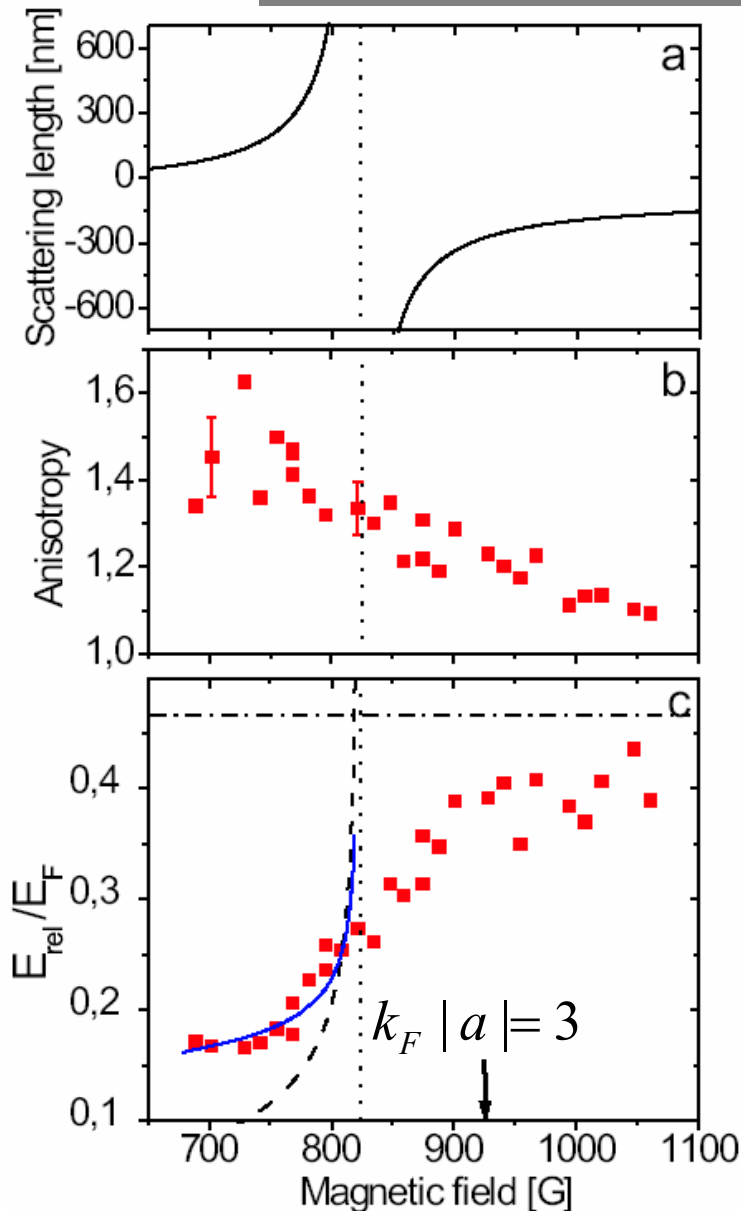
Prepare pure condensate: $4 \cdot 10^4$ molecules

Change magnetic field

Take 1.4 ms TOF image



Study of the crossover BEC -BCS



Anisotropy persists on $a < 0$ side
Composite Fermi-Bose system
near resonance.

At 820 Gauss,

$$\beta = E_{\text{int}} / E_{\text{kin}} = -0.55(10)$$

Mean field model with finite T

For $B = 720 \text{ G}$, $N_0 / N = 0.70$

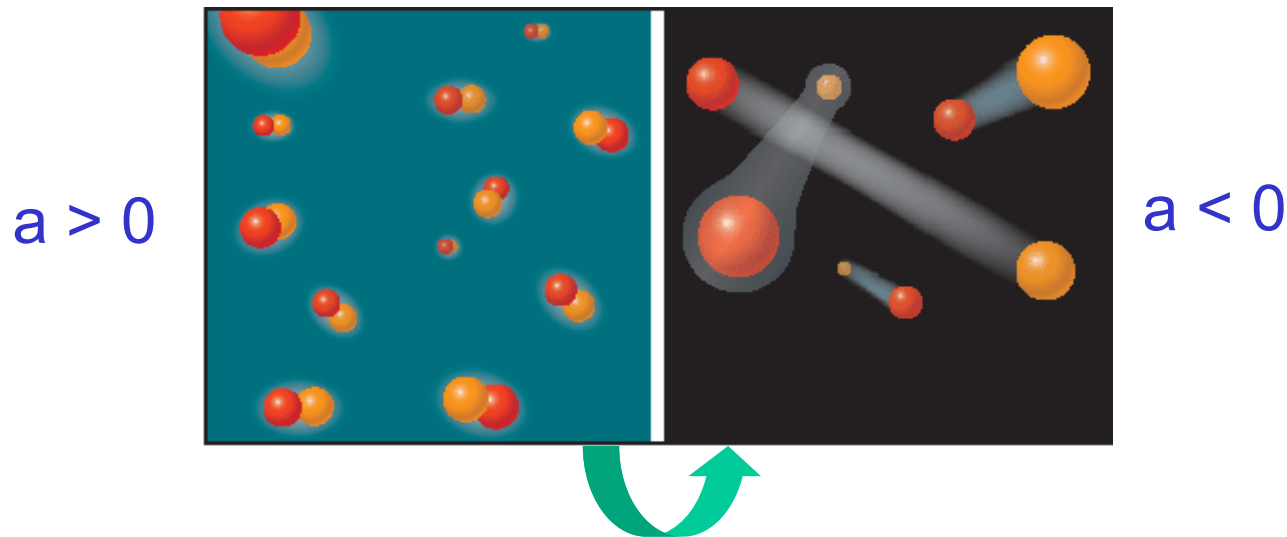
and $T = T_c^0 / 2 = 1.2 \mu\text{K}$

Fermi superfluid

Remains to be seen !

Produce BEC of molecules with $T/T_{\text{BEC}} \ll 1$

Cross the Feshbach resonance isentropically towards $a < 0$, currently $T/T_F < 0.1$.



According to L. Carr, G. Shlyapnikov and Y. Castin, cond-mat/0308306
this produces a deeply degenerate Fermi gas with $T = 0.01 T_F$ or lower !

Thus $T < T_{\text{BCS}}$ for $(k_F a)_{\text{final}} \sim 0.5$

Unambiguous detection of superfluid required !!

Perspectives

- Strongly interacting Fermions

BEC of molecules in the large a limit: non ideal effects

Analyze crossover Condensate of molecules/ superfluid Fermi gas
(Nozières, Randeria, Ohashi, Griffin)

- Search for clear signature of fermionic superfluidity

Theory of Fermi gas expansion

- Mott transition for fermions in an optical lattice (Hoffstetter et al.)

Simulate various many-body hamiltonians in periodic structures

Strongly correlated fermions domain is very vast !

- Bosons/fermions mixtures

- Collapse of Fermi gas observed in Firenze
- Pairing mechanism mediated by bosons
- Improve on T/T_F
- Better thermometry for $T/T_F \ll 1$